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A Operational Semantics

This appendix presents a big-step operational semantics for the simplified Lua language in Figure 3.3 as a series of inference rules for relations \xrightarrow{s} (statements and expression lists), \xrightarrow{l} (lvalues), and \xrightarrow{e} (expressions). Each relation is from a memory \mathcal{M} , an environment \mathcal{E} and a term a to another memory \mathcal{M}' and a value v that depends on the relation.

A memory \mathcal{M} is a function $\mathbf{Loc} \rightarrow \mathbf{Value} \cup \{\perp\}$. \mathbf{Loc} is the set of locations. \mathbf{Value} is the set of Lua values and also the set of output values of the relation \xrightarrow{e} . Lua values are numbers, strings, **nil**, **true**, **false**, closures, which are a pair of environment \mathcal{E} and function term f , and tables, which are locations pointing to functions $\mathbf{Value} \rightarrow \mathbf{Loc} \cup \{\perp\}$.

The set of output values for relation \xrightarrow{l} is \mathbf{Loc} , and for relation \xrightarrow{s} it is the set of value tuples \mathbf{Value}^* .

An environment \mathcal{E} is a function $\mathbf{Var} \rightarrow \mathbf{Loc}$ that maps variables to locations in memory.

The functions `index`, `app`, `arith` and `less` are primitives that model part of Lua's extensible semantics. The functions `index`, `arith` and `less` take a memory and two values and return a memory and a value, and `app` takes a memory, a value and a tuple and returns a memory and another tuple. The output memory of these functions is the same as the input memory for all locations that are \perp in the input memory and are not part of any of the input values.

A.1 Semantic Rules

Rule SKIP:

$$\mathcal{M}, \mathcal{E}, \mathbf{skip} \xrightarrow{s} \mathcal{M}, \perp$$

Rule SEQ-RETURN:

$$\frac{\mathcal{M}, \mathcal{E}, s_1 \xrightarrow{s} \mathcal{M}', v \quad v \neq \perp}{\mathcal{M}, \mathcal{E}, s_1; s_2 \xrightarrow{s} \mathcal{M}', v}$$

Rule SEQ:

$$\frac{\mathcal{M}, \mathcal{E}, s_1 \xrightarrow{s} \mathcal{M}', \perp \quad \mathcal{M}', \mathcal{E}, s_2 \xrightarrow{s} \mathcal{M}'', v}{\mathcal{M}, \mathcal{E}, s_1; s_2 \xrightarrow{s} \mathcal{M}'', v}$$

Rule RETURN:

$$\frac{\mathcal{M}, \mathcal{E}, el \xrightarrow{s} \mathcal{M}', v}{\mathcal{M}, \mathcal{E}, \mathbf{return} \, el \xrightarrow{s} \mathcal{M}', v}$$

Rule IF-FALSE:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', \mathbf{false} \quad \mathcal{M}', \mathcal{E}, s_2 \xrightarrow{s} \mathcal{M}'', v}{\mathcal{M}, \mathcal{E}, \mathbf{if} \, e \, \mathbf{then} \, s_1 \, \mathbf{else} \, s_2 \xrightarrow{s} \mathcal{M}'', v}$$

Rule IF-NIL:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', \mathbf{nil} \quad \mathcal{M}', \mathcal{E}, s_2 \xrightarrow{s} \mathcal{M}'', v}{\mathcal{M}, \mathcal{E}, \mathbf{if} \, e \, \mathbf{then} \, s_1 \, \mathbf{else} \, s_2 \xrightarrow{s} \mathcal{M}'', v}$$

Rule IF-TRUE:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', v \quad \mathcal{M}', \mathcal{E}, s_1 \xrightarrow{s} \mathcal{M}'', u \quad v \neq \mathbf{false} \quad v \neq \mathbf{nil}}{\mathcal{M}, \mathcal{E}, \mathbf{if} \, e \, \mathbf{then} \, s_1 \, \mathbf{else} \, s_2 \xrightarrow{s} \mathcal{M}'', u}$$

Rule WHILE-FALSE:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', \mathbf{false}}{\mathcal{M}, \mathcal{E}, \mathbf{while} \, e \, \mathbf{do} \, s \xrightarrow{s} \mathcal{M}', \perp}$$

Rule WHILE-FALSE:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', \mathbf{nil}}{\mathcal{M}, \mathcal{E}, \mathbf{while} \, e \, \mathbf{do} \, s \xrightarrow{s} \mathcal{M}', \perp}$$

Rule WHILE-RETURN:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', v \quad \mathcal{M}', \mathcal{E}, s \xrightarrow{s} \mathcal{M}'', u \quad v \neq \mathbf{false} \quad v \neq \mathbf{nil} \quad u \neq \perp}{\mathcal{M}, \mathcal{E}, \mathbf{while} \, e \, \mathbf{do} \, s \xrightarrow{s} \mathcal{M}'', u}$$

Rule WHILE-TRUE:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', v \quad \mathcal{M}', \mathcal{E}, s \xrightarrow{s} \mathcal{M}'', \perp \quad \mathcal{M}'', \mathcal{E}, \mathbf{while} \, e \, \mathbf{do} \, s \xrightarrow{s} \mathcal{M}''', u \quad v \neq \mathbf{false} \quad v \neq \mathbf{nil}}{\mathcal{M}, \mathcal{E}, \mathbf{while} \, e \, \mathbf{do} \, s \xrightarrow{s} \mathcal{M}''', u}$$

Rule LOCAL-1:

$$\frac{\mathcal{M}, \mathcal{E}, el \xrightarrow{s} \mathcal{M}', \perp \quad \mathcal{M}'[\vec{m} \mapsto \mathbf{nil}], \mathcal{E}[\vec{x} \mapsto \vec{m}], s \xrightarrow{s} \mathcal{M}'', v \quad \mathcal{M}'(m_k) = \perp}{\mathcal{M}, \mathcal{E}, \mathbf{local} \, \vec{x} = el \, \mathbf{in} \, s \xrightarrow{s} \mathcal{M}'', v}$$

Rule LOCAL-2:

$$\frac{\mathcal{M}, \mathcal{E}, el \xrightarrow{s} \mathcal{M}', \vec{v} \quad \mathcal{M}'[\vec{m} \mapsto \vec{v}_a], \mathcal{E}[\vec{x} \mapsto \vec{m}], s \xrightarrow{s} \mathcal{M}'', u \quad \mathcal{M}'(m_k) = \perp}{\mathcal{M}, \mathcal{E}, \mathbf{local} \vec{x} = el \mathbf{in} s \xrightarrow{s} \mathcal{M}'', v}$$

where $v_{a_k} = v_k$ if $k \leq |\vec{v}|$ and $v_{a_k} = \mathbf{nil}$ otherwise and $|\vec{m}| = |\vec{x}|$.

Rule ASSIGN-1:

$$\frac{\mathcal{M}, \mathcal{E}, l_1 \xrightarrow{l} \mathcal{M}_1, m_1 \dots \mathcal{M}_{k-1}, \mathcal{E}, l_k \xrightarrow{l} \mathcal{M}', m_k \quad \mathcal{M}', \mathcal{E}, el \xrightarrow{s} \mathcal{M}'', \perp}{\mathcal{M}, \mathcal{E}, \vec{l} = el \xrightarrow{s} \mathcal{M}''[\vec{m} \mapsto \vec{\mathbf{nil}}], \perp}$$

Rule ASSIGN-2:

$$\frac{\mathcal{M}, \mathcal{E}, l_1 \xrightarrow{l} \mathcal{M}_1, m_1 \dots \mathcal{M}_{k-1}, \mathcal{E}, l_k \xrightarrow{l} \mathcal{M}', m_k \quad \mathcal{M}', \mathcal{E}, el \xrightarrow{s} \mathcal{M}'', \vec{v}}{\mathcal{M}, \mathcal{E}, \vec{l} = el \xrightarrow{s} \mathcal{M}''[\vec{m} \mapsto \vec{v}_a], \perp}$$

where $v_{a_k} = v_k$ if $k \leq |\vec{v}|$ and $v_{a_k} = \mathbf{nil}$ otherwise and $|\vec{m}| = |\vec{l}|$.

Rule APP-STAT:

$$\frac{\mathcal{M}, \mathcal{E}, e(el)_1 \xrightarrow{e} \mathcal{M}', v}{\mathcal{M}, \mathcal{E}, e(el)_0 \xrightarrow{s} \mathcal{M}', \perp}$$

Rule VAR-LVAL:

$$\mathcal{M}, \mathcal{E}, x \xrightarrow{s} \mathcal{E}(x)$$

Rule VAR-RVAL:

$$\mathcal{M}, \mathcal{E}, x \xrightarrow{e} \mathcal{M}(\mathcal{E}(x))$$

Rule CONS:

$$\mathcal{M}, \mathcal{E}, \{\} \xrightarrow{e} \mathcal{M}[t \mapsto \lambda x. \perp], t \quad \mathcal{M}(t) = \perp$$

Rule TAB-LVAL:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', t \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v \quad t \in \mathbf{Table} \quad \mathcal{M}''(t)(v) \neq \perp}{\mathcal{M}, \mathcal{E}, e_1[e_2] \xrightarrow{s} \mathcal{M}'', \mathcal{M}''(t)(v)}$$

Rule TAB-LVAL-NEW:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', t \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v \quad t \in \mathbf{Table} \quad \mathcal{M}''(t)(v) = \perp}{\mathcal{M}, \mathcal{E}, e_1[e_2] \xrightarrow{s} \mathcal{M}''[t \mapsto \mathcal{M}''(t)[v \mapsto l], l \quad \mathcal{M}''(l) = \perp}$$

Rule TAB-RVAL:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', t \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v \quad t \in \mathbf{Table} \quad \mathcal{M}''(t)(v) \neq \perp}{\mathcal{M}, \mathcal{E}, e_1[e_2] \xrightarrow{s} \mathcal{M}'', \mathcal{M}''(\mathcal{M}''(t)(v))}$$

Rule TAB-RVAL-NIL:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', t \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v \quad t \in \mathbf{Table} \quad \mathcal{M}''(t)(v) = \perp}{\mathcal{M}, \mathcal{E}, e_1[e_2] \xrightarrow{s} \mathcal{M}'', \mathbf{nil}}$$

Rule TAB-META:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v_2 \quad v_1 \notin \mathbf{Table}}{\mathcal{M}, \mathcal{E}, e_1[e_2] \xrightarrow{e} \mathbf{index}(\mathcal{M}'', v_1, v_2)}$$

Rule EL-EMPTY:

$$\mathcal{M}, \mathcal{E}, \mathbf{nothing} \xrightarrow{s} \mathcal{M}, \perp$$

Rule EL:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}_1, v_1 \dots \mathcal{M}_{k-1}, \mathcal{E}, e_k \xrightarrow{e} \mathcal{M}', v_k \quad k = |\vec{v}|}{\mathcal{M}, \mathcal{E}, \vec{e} \xrightarrow{s} \mathcal{M}', \vec{v}}$$

Rule EL-MEXP:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}_1, v_1 \dots \mathcal{M}_{k-1}, \mathcal{E}, e_k \xrightarrow{e} \mathcal{M}', v_k \quad \mathcal{M}', \mathcal{E}, me \xrightarrow{s} \mathcal{M}'', u \quad k = |\vec{v}|}{\mathcal{M}, \mathcal{E}, \vec{e}, me \xrightarrow{s} \mathcal{M}'', \vec{v}u}$$

Rule APP-CLOSURE:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', \langle \mathcal{E}', \mathbf{fun}(\vec{x}) b \rangle \quad \mathcal{M}', \mathcal{E}, el \xrightarrow{s} \mathcal{M}'', \vec{v} \quad \mathcal{M}''[\vec{m} \mapsto \vec{v}_a], \mathcal{E}'[\vec{x} \mapsto \vec{m}], b \xrightarrow{s} \mathcal{M}''', u \quad \mathcal{M}''(m_k) = \perp}{\mathcal{M}, \mathcal{E}, e(el)_n \xrightarrow{s} \mathcal{M}''', u}$$

where $v_{a_k} = v_k$ if $k \leq |\vec{v}|$ and $v_{a_k} = \mathbf{nil}$ otherwise and $|\vec{m}| = |\vec{x}|$.

Rule APP-META:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, el \xrightarrow{s} \mathcal{M}'', v_2 \quad v_1 \notin \mathbf{Closure}}{\mathcal{M}, \mathcal{E}, e(el)_n \xrightarrow{s} \mathbf{app}(\mathcal{M}'', v_1, v_2)}$$

Rule APP-FIRST-NIL:

$$\frac{\mathcal{M}, \mathcal{E}, e(el)_n \xrightarrow{s} \mathcal{M}', \perp}{\mathcal{M}, \mathcal{E}, e(el)_1 \xrightarrow{e} \mathcal{M}', \mathbf{nil}}$$

Rule APP-FIRST:

$$\frac{\mathcal{M}, \mathcal{E}, e(el)_n \xrightarrow{s} \mathcal{M}', \vec{v}}{\mathcal{M}, \mathcal{E}, e(el)_1 \xrightarrow{e} \mathcal{M}', v_1}$$

Rule ARITH:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v_2 \quad v_1 \in \mathbf{Number} \quad v_2 \in \mathbf{Number}}{\mathcal{M}, \mathcal{E}, e_1 \oplus e_2 \xrightarrow{e} \mathcal{M}'', \mathcal{E}, v_1 \oplus v_2}$$

Rule ARITH-META:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v_2 \quad v_1 \notin \mathbf{Number} \vee v_2 \notin \mathbf{Number}}{\mathcal{M}, \mathcal{E}, e_1 \oplus e_2 \xrightarrow{e} \text{arith}(\mathcal{M}'', v_1, v_2)}$$

Rule EQ-TRUE:

$$\frac{\mathcal{M}, env, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} v_2 \quad v_1 = v_2}{\mathcal{M}, \mathcal{E}, e_1 == e_2 \xrightarrow{e} \mathcal{M}'', \mathbf{true}}$$

Rule EQ-FALSE:

$$\frac{\mathcal{M}, env, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} v_2 \quad v_1 \neq v_2}{\mathcal{M}, \mathcal{E}, e_1 == e_2 \xrightarrow{e} \mathcal{M}'', \mathbf{false}}$$

Rule LESS-TRUE:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v_2 \quad v_1 \in \mathbf{Number} \quad v_2 \in \mathbf{Number} \quad v_1 < v_2}{\mathcal{M}, \mathcal{E}, e_1 \oplus e_2 \xrightarrow{e} \mathcal{M}'', \mathcal{E}, \mathbf{true}}$$

Rule LESS-FALSE:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v_2 \quad v_1 \in \mathbf{Number} \quad v_2 \in \mathbf{Number} \quad v_1 \not< v_2}{\mathcal{M}, \mathcal{E}, e_1 \oplus e_2 \xrightarrow{e} \mathcal{M}'', \mathcal{E}, \mathbf{false}}$$

Rule LESS-META:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v_2 \quad v_1 \notin \mathbf{Number} \vee v_2 \notin \mathbf{Number}}{\mathcal{M}, \mathcal{E}, e_1 \oplus e_2 \xrightarrow{e} \text{less}(\mathcal{M}'', \mathcal{E}, v_1 \oplus v_2)}$$

Rule AND-NIL:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad v_1 = \mathbf{nil}}{\mathcal{M}, \mathcal{E}, e_1 \mathbf{and} e_2 \xrightarrow{e} \mathcal{M}', \mathbf{nil}}$$

Rule AND-FALSE:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad v_1 = \mathbf{false}}{\mathcal{M}, \mathcal{E}, e_1 \mathbf{and} e_2 \xrightarrow{e} \mathcal{M}', \mathbf{false}}$$

Rule AND:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v_2 \quad v_1 \neq \mathbf{false} \quad v_1 \neq \mathbf{nil}}{\mathcal{M}, \mathcal{E}, e_1 \mathbf{and} e_2 \xrightarrow{e} \mathcal{M}'', v_2}$$

Rule OR-NIL:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', \mathbf{nil} \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v_2}{\mathcal{M}, \mathcal{E}, e_1 \mathbf{or} e_2 \xrightarrow{e} \mathcal{M}'', v_2}$$

Rule OR-FALSE:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', \mathbf{false} \quad \mathcal{M}', \mathcal{E}, e_2 \xrightarrow{e} \mathcal{M}'', v_2}{\mathcal{M}, \mathcal{E}, e_1 \mathbf{or} e_2 \xrightarrow{e} \mathcal{M}'', v_2}$$

Rule OR:

$$\frac{\mathcal{M}, \mathcal{E}, e_1 \xrightarrow{e} \mathcal{M}', v_1 \quad v_1 \neq \mathbf{false} \quad v_1 \neq \mathbf{nil}}{\mathcal{M}, \mathcal{E}, e_1 \mathbf{or} e_2 \xrightarrow{e} \mathcal{M}', v_1}$$

Rule NOT-NIL:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', \mathbf{nil}}{\mathcal{M}, \mathcal{E}, \mathbf{not} e \xrightarrow{e} \mathcal{M}', \mathbf{true}}$$

Rule NOT-FALSE:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', \mathbf{false}}{\mathcal{M}, \mathcal{E}, \mathbf{not} e \xrightarrow{e} \mathcal{M}', \mathbf{true}}$$

Rule NOT-TRUE:

$$\frac{\mathcal{M}, \mathcal{E}, e \xrightarrow{e} \mathcal{M}', v \quad v \neq \mathbf{false} \quad v \neq \mathbf{nil}}{\mathcal{M}, \mathcal{E}, \mathbf{not} e \xrightarrow{e} \mathcal{M}', \mathbf{false}}$$

Rule FUN:

$$\mathcal{M}, \mathcal{E}, \mathbf{fun}(\vec{x}) b \xrightarrow{e} \mathcal{M}, \langle \mathcal{E}, \mathbf{fun}(\vec{x}) b \rangle$$

B Typing Rules

This appendix presents the full set of typing rules, including those already mentioned in Section 3.1.4.

Rule SKIP:

$$\Gamma \vdash \text{skip} : \text{void}$$

Rule SEQ-VOID:

$$\frac{\Gamma \vdash s_1 : \text{void} \quad \Gamma \vdash s_2 : \text{void}}{\Gamma \vdash s_1; s_2 : \text{void}}$$

Rule SEQ-1:

$$\frac{\Gamma \vdash s_1 : \tau \quad \Gamma \vdash s_2 : \text{void}}{\Gamma \vdash s_1; s_2 : \tau}$$

Rule SEQ-2:

$$\frac{\Gamma \vdash s_1 : \text{void} \quad \Gamma \vdash s_2 : \tau}{\Gamma \vdash s_1; s_2 : \tau}$$

Rule SEQ-BOTH:

$$\frac{\Gamma \vdash s_1 : \tau_1 \quad \Gamma \vdash s_2 : \tau_2 \quad \tau_1 \rightsquigarrow v \quad \tau_2 \rightsquigarrow v}{\Gamma \vdash s_1; s_2 : v}$$

Rule IF-VOID:

$$\frac{\Gamma \vdash e : \tau_e \quad \Gamma \vdash s_1 : \text{void} \quad \Gamma \vdash s_2 : \text{void}}{\Gamma \vdash \text{if } e \text{ then } s_1 \text{ else } s_2 : \text{void}}$$

Rule IF-1:

$$\frac{\Gamma \vdash e : \tau_e \quad \Gamma \vdash s_1 : \tau \quad \Gamma \vdash s_2 : \text{void}}{\Gamma \vdash \text{if } e \text{ then } s_1 \text{ else } s_2 : \tau}$$

Rule IF-2:

$$\frac{\Gamma \vdash e : \tau_e \quad \Gamma \vdash s_1 : \text{void} \quad \Gamma \vdash s_2 : \tau}{\Gamma \vdash \text{if } e \text{ then } s_1 \text{ else } s_2 : \tau}$$

Rule IF-BOTH:

$$\frac{\Gamma \vdash e : \tau_e \quad \Gamma \vdash s_1 : \tau_1 \quad \Gamma \vdash s_2 : \tau_2 \quad \tau_1 \rightsquigarrow v \quad \tau_2 \rightsquigarrow v}{\Gamma \vdash \text{if } e \text{ then } s_1 \text{ else } s_2 : v}$$

Rule WHILE-VOID:

$$\frac{\Gamma \vdash e : \tau \quad \Gamma \vdash s : \mathbf{void}}{\Gamma \vdash \mathbf{while } e \mathbf{ do } s : \mathbf{void}}$$

Rule WHILE:

$$\frac{\Gamma \vdash e : \tau \quad \Gamma \vdash s : v}{\Gamma \vdash \mathbf{while } e \mathbf{ do } s : v}$$

Rule RETURN:

$$\frac{\Gamma \vdash el : \tau \quad \tau \rightsquigarrow v}{\Gamma \vdash \mathbf{return } el : v}$$

Rule LOCAL-DROP-VOID:

$$\frac{\Gamma \vdash el : v_1 \times \dots \times v_m \quad \Gamma[\vec{x} \mapsto \vec{\tau}] \vdash s : \mathbf{void} \quad m \geq |\vec{x}| \quad v_k \rightsquigarrow \tau_k}{\Gamma \vdash \mathbf{local } \vec{x} = el \mathbf{ in } s : \mathbf{void}}$$

Rule LOCAL-DROP:

$$\frac{\Gamma \vdash el : v_1 \times \dots \times v_m \quad \Gamma[\vec{x} \mapsto \vec{\tau}] \vdash s : \omega \quad m \geq |\vec{x}| \quad v_k \rightsquigarrow \tau_k}{\Gamma \vdash \mathbf{local } \vec{x} = el \mathbf{ in } s : \omega}$$

Rule LOCAL-FILL-VOID:

$$\frac{\Gamma \vdash el : v_1 \times \dots \times v_m \quad \Gamma[\vec{x} \mapsto \vec{\tau}] \vdash s : \mathbf{void} \quad m < |\vec{x}| \quad v_k \rightsquigarrow \tau_k \quad \mathbf{nil} \rightsquigarrow \tau_l \quad l > m}{\Gamma \vdash \mathbf{local } \vec{x} = el \mathbf{ in } s : \mathbf{void}}$$

Rule LOCAL-FILL:

$$\frac{\Gamma \vdash el : v_1 \times \dots \times v_m \quad \Gamma[\vec{x} \mapsto \vec{\tau}] \vdash s : \omega \quad m < |\vec{x}| \quad v_k \rightsquigarrow \tau_k \quad \mathbf{nil} \rightsquigarrow \tau_l \quad l > m}{\Gamma \vdash \mathbf{local } \vec{x} = el \mathbf{ in } s : \omega}$$

Rule LOCAL-VAR-DROP-VOID:

$$\frac{\Gamma \vdash el : v_1 \times \dots \times v_m \times \mathcal{D}^* \quad \Gamma[\vec{x} \mapsto \vec{\tau}] \vdash s : \mathbf{void} \quad m \geq |\vec{x}| \quad v_k \rightsquigarrow \tau_k}{\mathbf{flocal } \vec{x} = el \mathbf{ in } s : \mathbf{void}}$$

Rule LOCAL-VAR-DROP:

$$\frac{\Gamma \vdash el : v_1 \times \dots \times v_m \times \mathcal{D}^* \quad \Gamma[\vec{x} \mapsto \vec{\tau}] \vdash s : \omega \quad m \geq |\vec{x}| \quad v_k \rightsquigarrow \tau_k}{\mathbf{flocal } \vec{x} = el \mathbf{ in } s : \omega}$$

Rule LOCAL-VAR-FILL-VOID:

$$\frac{\Gamma \vdash el : v_1 \times \dots \times v_m \times \mathcal{D}^* \quad \Gamma[\vec{x} \mapsto \vec{\tau}] \vdash s : \mathbf{void} \quad m < |\vec{x}| \quad v_k \rightsquigarrow \tau_k \quad \tau_l = \mathcal{D} \quad l > m}{\Gamma \vdash \mathbf{local } \vec{x} = el \mathbf{ in } s : \mathbf{void}}$$

Rule LOCAL-VAR-FILL:

$$\frac{\Gamma \vdash el : v_1 \times \dots \times v_m \times \mathcal{D}^* \quad \Gamma[\vec{x} \mapsto \vec{\tau}] \vdash s : \omega \quad m < |\vec{x}| \quad v_k \rightsquigarrow \tau_k \quad \tau_l = \mathcal{D} \quad l > m}{\Gamma \vdash \mathbf{local} \vec{x} = el \mathbf{in} s : \omega}$$

Rule ASSIGN-DROP:

$$\frac{\Gamma \vdash l_k : \tau_k \quad \Gamma \vdash el : v_1 \times \dots \times v_m \quad m \geq |\vec{l}| \quad v_k \rightsquigarrow \tau_k}{\Gamma \vdash \vec{l} = el : \mathbf{void}}$$

Rule ASSIGN-FILL:

$$\frac{\Gamma \vdash l_k : \tau_k \quad \Gamma \vdash el : v_1 \times \dots \times v_m \quad m < |\vec{l}| \quad v_k \rightsquigarrow \tau_k \quad \mathbf{nil} \rightsquigarrow \tau_l \quad l > m}{\Gamma \vdash \vec{l} = el : \mathbf{void}}$$

Rule ASSIGN-VAR-DROP:

$$\frac{\Gamma \vdash l_k : \tau_k \quad \Gamma \vdash el : v_1 \times \dots \times v_m \times \mathcal{D}^* \quad m \geq |\vec{l}| \quad v_k \rightsquigarrow \tau_k}{\Gamma \vdash \vec{l} = el : \mathbf{void}}$$

Rule ASSIGN-VAR-FILL:

$$\frac{\Gamma \vdash l_k : \tau_k \quad \Gamma \vdash el : v_1 \times \dots \times v_m \times \mathcal{D}^* \quad m < |\vec{l}| \quad v_k \rightsquigarrow \tau_k \quad \tau_l = \mathcal{D} \quad l > m}{\Gamma \vdash \vec{l} = el : \mathbf{void}}$$

Rule EL-EMPTY:

$$\overline{\Gamma \vdash \mathbf{nothing} : \mathbf{empty}}$$

Rule EL:

$$\frac{\Gamma \vdash e_k : \tau_k \quad n = |\vec{e}|}{\Gamma \vdash \vec{e} : \tau_1 \times \dots \times \tau_n}$$

Rule EL-MEXP-EMPTY:

$$\frac{\Gamma \vdash e_k : \tau_k \quad \Gamma \vdash me : \mathbf{empty} \quad n = |\vec{e}|}{\Gamma \vdash \vec{e}, me : \tau_1 \times \dots \times \tau_n}$$

Rule EL-MEXP:

$$\frac{\Gamma \vdash e_k : \tau_k \quad \Gamma \vdash me : v_1 \times \dots \times v_m \quad n = |\vec{e}|}{\Gamma \vdash \vec{e}, me : \tau_1 \times \dots \times \tau_n \times v_1 \times \dots \times v_m}$$

Rule EL-VAR-1:

$$\frac{\Gamma \vdash e_k : \tau_k \quad \Gamma \vdash me : \mathcal{D}^* \quad n = |\vec{e}|}{\Gamma \vdash \vec{e}, me : \tau_1 \times \dots \times \tau_n \times \mathcal{D}^*}$$

Rule EL-VAR-2:

$$\frac{\Gamma \vdash e_k : \tau_k \quad \Gamma \vdash me : v_1 \times \dots \times v_m \times \mathcal{D}^* \quad n = |\vec{e}|}{\Gamma \vdash \vec{e}, me : \tau_1 \times \dots \times \tau_n \times v_1 \times \dots \times v_m \times \mathcal{D}^*}$$

Rule APP-DROP:

$$\frac{\Gamma \vdash f : \tau_1 \times \dots \times \tau_n \rightarrow \sigma \quad \Gamma \vdash el : v_1 \times \dots \times v_m \quad m \geq n \quad v_k \rightsquigarrow \tau_k}{\Gamma \vdash f(el)_n : \sigma}$$

Rule APP-FILL:

$$\frac{\Gamma \vdash f : \tau_1 \times \dots \times \tau_n \rightarrow \sigma \quad \Gamma \vdash el : v_1 \times \dots \times v_m \quad m < n \quad v_k \rightsquigarrow \tau_k \quad \mathbf{nil} \rightsquigarrow \tau_l \quad l > m}{\Gamma \vdash f(el)_n : \sigma}$$

Rule APP-VAR-DROP:

$$\frac{\Gamma \vdash f : \tau_1 \times \dots \times \tau_n \rightarrow \sigma \quad \Gamma \vdash el : v_1 \times \dots \times v_m \times \mathcal{D}^* \quad m \geq n \quad v_k \rightsquigarrow \tau_k}{\Gamma \vdash f(el)_n : \sigma}$$

Rule APP-VAR-FILL:

$$\frac{\Gamma \vdash f : \tau_1 \times \dots \times \tau_n \rightarrow \sigma \quad \Gamma \vdash el : v_1 \times \dots \times v_m \times \mathcal{D}^* \quad m < n \quad v_k \rightsquigarrow \tau_k \quad \tau_l = \mathcal{D} \quad l > m}{\Gamma \vdash f(el)_n : \sigma}$$

Rule APP-DYN:

$$\frac{\Gamma \vdash f : \tau \quad \Gamma \vdash el : v \quad \tau \rightsquigarrow \mathcal{D} \quad v \rightsquigarrow \mathcal{D}^*}{\Gamma \vdash f(el)_n : \mathcal{D}^*}$$

Rule APP-STAT:

$$\frac{\Gamma \vdash e(el)_n : \tau}{\Gamma \vdash e(el)_0 : \mathbf{void}}$$

Rule APP-FIRST:

$$\frac{\Gamma \vdash e(el)_n : \tau_1 \times \dots \times \tau_n}{\Gamma \vdash e(el)_1 : \tau_1}$$

Rule APP-FIRST-NIL:

$$\frac{\Gamma \vdash e(el)_n : \mathbf{empty}}{\Gamma \vdash e(el)_1 : \mathbf{nil}}$$

Rule APP-FIRST-DYN:

$$\frac{\Gamma \vdash e(el)_n : \mathcal{D}^*}{\Gamma \vdash e(el)_1 : \mathcal{D}}$$

Rule CONS:

$$\frac{\forall i, j, \sigma. (i \neq j \wedge \sigma \rightsquigarrow \tau_i) \rightarrow \sigma \not\rightsquigarrow \tau_j \quad \mathbf{nil} \rightsquigarrow v_k}{\Gamma \vdash \{\}: \tau_1 \mapsto v_1 \wedge \dots \wedge \tau_n \mapsto v_n}$$

Rule CONS-DYN:

$$\frac{\mathbf{nil} \rightsquigarrow v}{\Gamma \vdash \{\}: \mathcal{D} \mapsto v}$$

Rule INDEX:

$$\frac{\Gamma \vdash e_1 : \tau_1 \mapsto v_1 \wedge \dots \wedge \tau_n \mapsto v_n \quad \Gamma \vdash e_2 : \sigma \quad \sigma \rightsquigarrow \tau_k}{\Gamma \vdash e_1[e_2] : v_k}$$

Rule INDEX-DYN:

$$\frac{\Gamma \vdash e_1 : \tau \quad \Gamma \vdash e_2 : v \quad \tau \rightsquigarrow \mathcal{D} \quad v \rightsquigarrow \mathcal{D}}{\Gamma \vdash e_1[e_2] : \mathcal{D}}$$

Rule ARITH-NUM:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_1 \rightsquigarrow \mathbf{Number} \quad \tau_2 \rightsquigarrow \mathbf{Number}}{\Gamma \vdash e_1 \oplus e_2 : \mathbf{Number}}$$

Rule ARITH-DYN:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_1 \not\rightsquigarrow \mathbf{Number} \vee \tau_2 \not\rightsquigarrow \mathbf{Number} \quad \tau_1 \rightsquigarrow \mathcal{D} \quad \tau_2 \rightsquigarrow \mathcal{D}}{\Gamma \vdash e_1 \oplus e_2 : \mathcal{D}}$$

Rule EQ:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_1 \rightsquigarrow \tau_2 \vee \tau_2 \rightsquigarrow \tau_1}{\Gamma \vdash e_1 == e_2 : \mathbf{Bool}}$$

Rule LESS-NUM:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_1 \rightsquigarrow \mathbf{Number} \quad \tau_2 \rightsquigarrow \mathbf{Number}}{\Gamma \vdash e_1 < e_2 : \mathbf{Bool}}$$

Rule LESS-DYN:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_1 \not\rightsquigarrow \mathbf{Number} \vee \tau_2 \not\rightsquigarrow \mathbf{Number} \quad \tau_1 \rightsquigarrow \mathcal{D} \quad \tau_2 \rightsquigarrow \mathcal{D}}{\Gamma \vdash e_1 < e_2 : \mathcal{D}}$$

Rule AND-NIL:

$$\frac{\Gamma \vdash e_1 : \mathbf{nil}}{\Gamma \vdash e_1 \mathbf{and} e_2 : \mathbf{nil}}$$

Rule AND-FALSE:

$$\frac{\Gamma \vdash e_1 : \mathbf{false}}{\Gamma \vdash e_1 \mathbf{and} e_2 : \mathbf{false}}$$

Rule AND-TRUE:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_1 \neq \mathbf{false} \quad \mathbf{nil} \not\rightsquigarrow \tau_1}{\Gamma \vdash e_1 \mathbf{and} e_2 : \tau_2}$$

Rule AND:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_1 \neq \mathbf{nil} \quad \mathbf{nil} \rightsquigarrow \tau_1 \quad \tau_1 \rightsquigarrow v \quad \tau_2 \rightsquigarrow v}{\Gamma \vdash e_1 \mathbf{and} e_2 : v}$$

Rule OR-NIL:

$$\frac{\Gamma \vdash e_1 : \mathbf{nil} \quad \Gamma \vdash e_2 : \tau}{\Gamma \vdash e_1 \mathbf{or} e_2 : \tau}$$

Rule OR-FALSE:

$$\frac{\Gamma \vdash e_1 : \mathbf{false} \quad \Gamma \vdash e_2 : \tau}{\Gamma \vdash e_1 \mathbf{or} e_2 : \tau}$$

Rule OR-TRUE:

$$\frac{\Gamma \vdash e_1 : \tau \quad \tau \neq \mathbf{false} \quad \mathbf{nil} \not\rightsquigarrow \tau}{\Gamma \vdash e_1 \mathbf{or} e_2 : \tau}$$

Rule OR:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_1 \neq \mathbf{nil} \quad \mathbf{nil} \rightsquigarrow \tau_1 \quad \tau_1 \rightsquigarrow v \quad \tau_2 \rightsquigarrow v}{\Gamma \vdash e_1 \mathbf{or} e_2 : v}$$

Rule NOT-NIL:

$$\frac{\Gamma \vdash e : \mathbf{nil}}{\Gamma \vdash \mathbf{not} e : \mathbf{true}}$$

Rule NOT-FALSE:

$$\frac{\Gamma \vdash e : \mathbf{false}}{\Gamma \vdash \mathbf{not} e : \mathbf{true}}$$

Rule NOT-TRUE:

$$\frac{\Gamma \vdash e : t \quad t \neq \mathbf{false} \quad \mathbf{nil} \not\rightsquigarrow t}{\Gamma \vdash \mathbf{not} e : \mathbf{false}}$$

Rule NOT:

$$\frac{\Gamma \vdash e : t \quad t \neq \mathbf{nil} \quad \mathbf{nil} \rightsquigarrow t}{\Gamma \vdash \mathbf{not} e : \mathbf{Bool}}$$

Rule FUN-EMPTY:

$$\frac{\Gamma \vdash s; \mathbf{return} el : v}{\Gamma \vdash \mathbf{fun}() s; \mathbf{return} el : \tau_1 \times \dots \times \tau_n \rightarrow v}$$

Rule FUN:

$$\frac{\Gamma[\vec{x} \mapsto \vec{\tau}] \vdash s; \mathbf{return} el : v}{\Gamma \vdash \mathbf{fun}(\vec{x}) s; \mathbf{return} el : \tau_1 \times \dots \times \tau_n \rightarrow v \quad n \geq |\vec{x}|}$$

C Collected Benchmark Results

	base	single	box	intern	prop	infer
binary-trees	2.140	1.987	2.256	1.143	0.857	0.193
fannkuch	1.825	1.835	3.315	3.397	1.684	0.829
fib-iter	0.567	0.504	1.780	1.824	0.130	0.062
fib-memo	0.468	0.230	0.318	0.340	0.351	0.147
fib-rec	1.806	0.540	1.311	1.297	1.304	0.773
mandelbrot	1.632	1.588	5.608	5.551	0.146	0.145
n-body	2.656	2.516	4.169	3.123	3.084	0.853
n-sieve	1.901	1.887	3.115	3.138	1.352	0.296
nsieve-bits	0.883	0.567	1.377	1.403	1.028	0.574
partial-sum	0.647	0.493	1.152	1.184	0.680	0.407
recursive	1.639	0.450	1.418	1.425	1.488	0.110
spectral-norm	1.894	1.186	3.212	3.245	3.175	0.210
richards	0.343	0.308	0.329	0.217	0.202	0.047
richards-tail	N/A	N/A	N/A	N/A	N/A	N/A
richards-oo	0.383	0.304	0.327	0.227	0.197	0.052
richards-oo-tail	N/A	N/A	N/A	N/A	N/A	N/A
richards-oo-meta	0.691	0.634	0.463	0.315	0.274	0.242
richards-oo-cache	0.493	0.352	0.370	0.241	0.216	0.186

Table C.1: Benchmark running times for Mono 2.4, in seconds

	base	single	box	intern	prop	infer
binary-trees	0.686	0.671	0.686	0.269	0.218	0.031
fannkuch	1.373	1.392	1.267	1.312	0.895	0.696
fib-iter	0.189	0.189	0.236	0.232	0.037	0.029
fib-memo	0.183	0.156	0.154	0.176	0.166	0.023
fib-rec	0.920	0.644	0.287	0.265	0.265	0.131
mandelbrot	1.102	1.115	0.858	0.985	0.037	0.041
n-body	1.952	1.798	1.817	1.277	1.197	0.191
n-sieve	1.336	1.326	1.244	1.258	0.996	0.205
n-sieve-bits	0.365	0.343	0.359	0.363	0.296	0.199
partial-sum	0.314	0.291	0.283	0.269	0.168	0.158
recursive	0.712	0.511	0.253	0.242	0.222	0.047
spectral-norm	1.178	1.125	0.840	0.850	0.825	0.162
richards	0.240	0.230	0.211	0.156	0.148	0.055
richards-tail	0.255	0.234	0.215	0.160	0.150	0.064
richards-oo	0.255	0.218	0.201	0.158	0.127	0.055
richards-oo-tail	N/A	N/A	1.094	0.827	0.628	0.060
richards-oo-meta	0.425	0.398	0.298	0.211	0.201	0.179
richards-oo-cache	0.281	0.252	0.240	0.162	0.156	0.152

Table C.2: Benchmark running times for .NET 3.5 SP1, in seconds

	base	single	box	intern	prop	infer
binary-trees	0.691	0.690	0.597	0.252	0.203	0.035
fannkuch	1.182	1.406	1.196	1.301	0.895	0.671
fib-iter	0.204	0.218	0.243	0.268	0.044	0.034
fib-memo	0.178	0.165	0.150	0.172	0.173	0.029
fib-rec	0.968	0.665	0.318	0.297	0.296	0.138
mandelbrot	1.093	1.120	1.007	0.998	0.042	0.045
n-body	1.747	1.986	1.658	1.303	1.190	0.183
n-sieve	1.437	1.450	1.292	1.259	0.983	0.206
nsieve-bits	0.346	0.356	0.354	0.381	0.318	0.193
partial-sum	0.331	0.304	0.281	0.283	0.180	0.161
recursive	0.735	0.525	0.277	0.266	0.258	0.052
spectral-norm	1.152	1.131	0.854	0.873	0.848	0.107
richards	0.280	0.259	0.217	0.159	0.152	0.050
richards-tail	0.278	0.261	0.214	0.162	0.156	0.063
richards-oo	0.279	0.263	0.201	0.158	0.140	0.054
richards-oo-tail	N/A	N/A	1.212	0.690	0.394	0.055
richards-oo-meta	0.470	0.460	0.291	0.207	0.202	0.190
richards-oo-cache	0.308	0.283	0.228	0.169	0.162	0.152

Table C.3: Benchmark running times for .NET 4.0 Beta 1, in seconds

	lua	luajit
binary-trees	0.259	0.184
fannkuch	1.228	0.707
fib-iter	0.499	0.083
fib-memo	0.264	0.109
fib-rec	0.835	0.170
mandelbrot	0.503	0.108
n-body	0.680	0.347
n-sieve	0.655	0.532
n-sieve-bits	0.318	0.134
partial-sum	0.282	0.136
recursive	0.704	0.128
spectra-lnorm	0.705	0.269
richards	0.133	0.054
richards-tail	0.137	0.059
richards-oo	0.116	0.052
richards-oo-tail	0.128	0.056
richards-oo-meta	0.140	0.068
richards-oo-cache	0.138	0.062

Table C.4: Benchmark running times for Lua 5.1.4 and LuaJIT 1.1.5, in seconds

binary-trees	0.137
fannkuch	1.983
fib-iter	0.553
fib-memo	0.102
fib-rec	0.706
mandelbrot	1.061
n-body	1.581
n-sieve	0.753
n-sieve-bits	0.626
partial-sum	0.402
recursive	0.476
spectral-norm	1.838
richards	0.676

Table C.5: Benchmark running times for IronPython 2.0, in seconds